# Squashing 

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## References:

- "Multi-score Position Auctions" (Charles et al. (2016) WSDM'16)
- "Revenue Analysis of a Family of Ranking Rules for Keyword Auctions" (Lahaie and Pennock (2007) EC'07)
- "A Structural Model of Sponsored Search Advertising Auctions" (Athey and Nekipelov (2011) Working Paper)


## Squashing + GSP:

- Let $b_{1}, b_{2}, \ldots, b_{1}$ advertisers bids
- Let $s_{1}^{\theta}, s_{2}^{\theta}, \ldots, s_{l}^{\theta}$ scores
- $s_{i}$ : clickability measure
- $\theta$ : squashing factor


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- GSP ranking
- Order ads based on $s_{i} \times b_{i}$
- GSP + Squashing ranking
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\text { Price }_{1}=\frac{b_{2} \times s_{2}^{\theta}}{s_{1}^{\theta}}
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- If $\theta=0$ then Price $_{1}=b_{2}$
- If $\theta=1$ then Price $_{1}=b_{2} \times s_{2} / s_{1}$


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- Expected Cost : eCost ${ }_{1}=$ Price $_{1} \times$ CTR $_{1}$.


## Revenue Impact: Scenario 1

- GSP order $=$ Squashed GSP order $=$ Click-probability order
- 2 bidders and zero reserve price


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Bid1 \& Bid2 $=\mathbf{\$ 1 , e C T R 1 = 0 . 5 , e C T R 2 = 0 . 3 3}$


## Revenue Impact: Scenario 2

- GSP order $=$ Squashed GSP order $\neq$ Click-probability order
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Bid1=\$10,Bid2 = \$1,eCTR1=0.5,eCTR2=0.66


## Revenue Impact: Scenario 3

- GSP order $=$ Click-probability order $\neq$ Squashed GSP order
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- GSP order $=$ Click-probability order $\neq$ Squashed GSP order
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Bid1=\$1,Bid2 = \$1.6,eCTR1=0.5,eCTR2=0.17


